1.

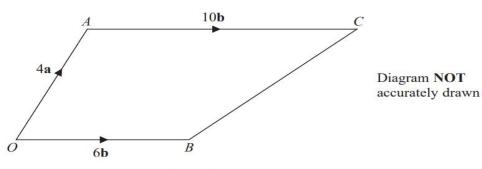


Figure 4

Figure 4 shows a trapezium OACB.

$$\overrightarrow{OA} = 4\mathbf{a}$$
 $\overrightarrow{OB} = 6\mathbf{b}$ $\overrightarrow{AC} = 10\mathbf{b}$

P is the point on AB such that OPC is a straight line.

Find an expression for \overrightarrow{PC} in terms of **a** and **b**. Give your answer in its simplest form.

(6)

June2020/Q7

2.

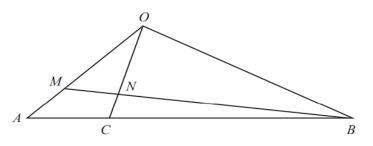


Diagram **NOT** accurately drawn

Figure 2

Figure 2 shows the triangle \overrightarrow{OAB} in which $\overrightarrow{OA} = 3\mathbf{a}$ and $\overrightarrow{OB} = 15\mathbf{b}$

C is the point on AB such that $\overrightarrow{AC} = \frac{1}{3} \overrightarrow{AB}$

N is the point on OC such that $\overrightarrow{ON} = \frac{3}{4} \overrightarrow{OC}$

(a) Find and simplify an expression for \overrightarrow{BN} in terms of **a** and **b**

(3)

M is the point on OA such that B, N and M are collinear.

(b) Find the ratio *OM* : *MA* Show your working clearly.

(F)

June2023/12

3.

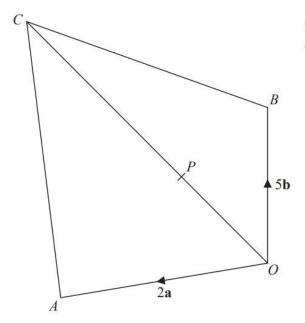


Diagram **NOT** accurately drawn

Figure 1

In Figure 1, OACB is a quadrilateral in which $\overrightarrow{OA} = 2\mathbf{a}$ and $\overrightarrow{OB} = 5\mathbf{b}$

(a) Find \overrightarrow{AB} in terms of **a** and **b**

(1)

P is the point on OC such that OP : PC = 1 : 4

Given that $\overrightarrow{BC} = 6\mathbf{a} + 5\mathbf{b}$

- (b) (i) prove that A, P and B are collinear,
 - (ii) find a value of m and a value of n such that AP : PB = m : n

(5)

June2021/Q4

4.

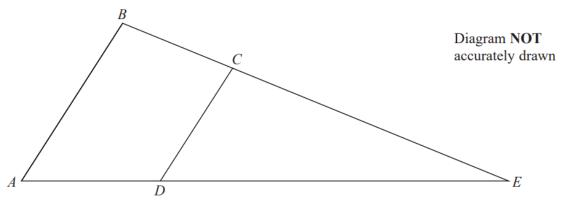


Figure 1

Figure 1 shows quadrilateral ABCD such that $\overrightarrow{AB} = \mathbf{a}$ and $\overrightarrow{AD} = \mathbf{b}$

E is the point such that ADE and BCE are straight lines.

Given that $\overrightarrow{BC} = \mathbf{b} - \frac{1}{3}\mathbf{a}$

(a) show that AB is parallel to DC

(2)

Given also that λ is a scalar such that $\overrightarrow{BE} = \lambda \mathbf{b} - \mathbf{a}$

(b) find the value of λ

(2)

The area of triangle ABE is x square units.

Given that the area of quadrilateral ABCD is P square units,

(c) find an expression for P in terms of x

(3)

June2022/Q7

5.

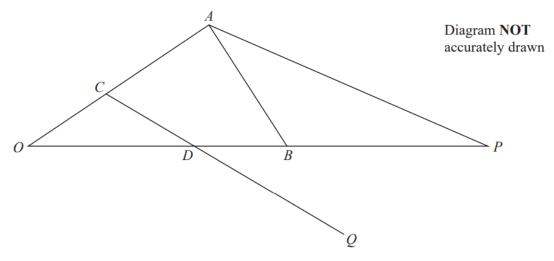


Figure 2

Figure 2 shows the triangle \overrightarrow{OAB} with $\overrightarrow{OA} = 2\mathbf{a}$ and $\overrightarrow{OB} = 3\mathbf{b}$

The point C lies on OA such that $\overrightarrow{OC} = \frac{1}{3} \overrightarrow{OA}$

The point *D* lies on *OB* such that $\overrightarrow{OD} = \frac{2}{3} \overrightarrow{OB}$

(a) Find \overrightarrow{CD} in terms of **a** and **b**.

(2)

The point P is such that ODBP is a straight line and AP is parallel to CD.

(b) Find \overrightarrow{OP} in terms of **b**.

(4)

The point Q is such that $\overrightarrow{CD} = \overrightarrow{DQ}$

(c) Show that A, B and Q are collinear.

(4)

January 2019/Q8

6.

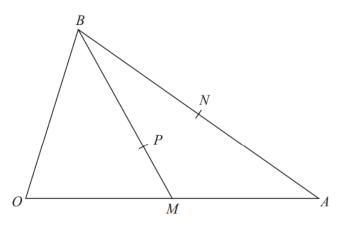


Diagram **NOT** accurately drawn

Figure 3

Figure 3 shows the triangle \overrightarrow{OAB} where $\overrightarrow{OA} = 12\mathbf{a}$ and $\overrightarrow{OB} = 6\mathbf{b}$ M is the midpoint of OA and N is the midpoint of AB.

The point P on BM is such that BP : BM = 2 : 3

- (a) Simplifying your answer, find, in terms of a and b
 - (i) \overrightarrow{BM}
- (ii) \overrightarrow{OP}

(3)

(b) Hence show that O, P and N are collinear.

(4)

Given that $|\mathbf{a}| = |\mathbf{b}| = 1 \text{ cm}$ and that $\angle AOB = 70^{\circ}$

(c) find the length, in cm to 3 significant figures, of OP.

(3)

January 2021/Q10

7.

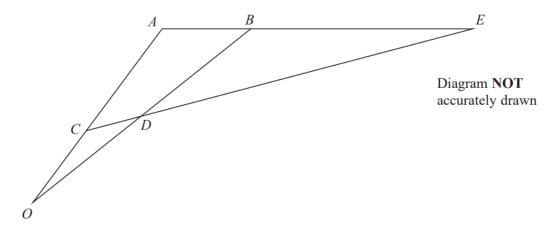


Figure 1

Figure 1 shows triangle OAB

Given that $\overrightarrow{OA} = \mathbf{a}$ and $\overrightarrow{OB} = \mathbf{b}$

(a) find \overrightarrow{AB} in terms of **a** and **b**

(1)

The point C lies on OA such that OC: OA = 1:3

The point *D* lies on *OB* such that $\overrightarrow{OD} = \frac{2}{5} \overrightarrow{OB}$

Given that the point E is such that ABE and CDE are straight lines,

(b) find and simplify an expression, in terms of **a** and **b**, for \overrightarrow{AE}

(6)

January 2022/Q5

8.

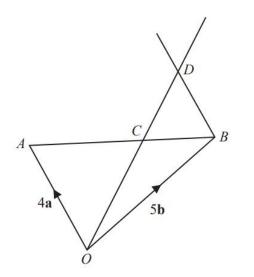


Diagram **NOT** accurately drawn

Figure 4

Figure 4 shows triangle *OAB*

The point C lies on AB such that $AC = \frac{3}{5}AB$

Given that $\overrightarrow{OA} = 4\mathbf{a}$ and $\overrightarrow{OB} = 5\mathbf{b}$

(a) find an expression for \overrightarrow{OC} in terms of **a** and **b** Give your answer in its simplest form.

(3)

The point *D* is such that *OCD* is a straight line.

Given that BD is parallel to OA

(b) use a vector method to find an expression for \overrightarrow{OD} in terms of **a** and **b** Give your answer in its simplest form.

(4)

January 2023/Q6

9.

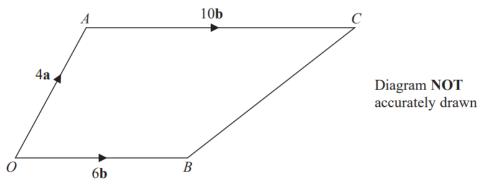


Figure 4

Figure 4 shows a trapezium OACB.

$$\overrightarrow{OA} = 4\mathbf{a}$$
 $\overrightarrow{OB} = 6\mathbf{b}$ $\overrightarrow{AC} = 10\mathbf{b}$

P is the point on AB such that OPC is a straight line.

Find an expression for \overrightarrow{PC} in terms of **a** and **b**. Give your answer in its simplest form.

October2020/Q7

10.

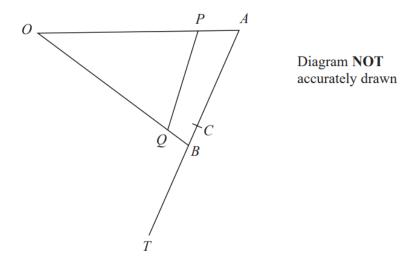


Figure 3

Figure 3 shows the triangle \overrightarrow{OAB} in which $\overrightarrow{OA} = 4\mathbf{a}$ and $\overrightarrow{OB} = 6\mathbf{b}$

C is the point on AB such that AC: CB = 3:1

(a) Find and simplify an expression for \overrightarrow{OC} in terms of **a** and **b**.

(3)

The point T is such that ABT is a straight line and AC = CT.

The point *P* is such that $\overrightarrow{OP} = \frac{3}{4} \overrightarrow{OA}$

Q is the point on OB such that the points P, Q and T are collinear.

Given that OQ: QB = n:1

(b) find the value of n.

(4)

October 2021/Q10

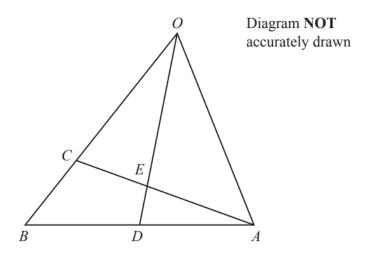


Figure 2

Figure 2 shows triangle \overrightarrow{OAB} with $\overrightarrow{OA} = 4\mathbf{a}$ and $\overrightarrow{OB} = 3\mathbf{b}$

The point C lies on OB such that $\overrightarrow{OC} = 2\mathbf{b}$

The point D is the midpoint of AB

The point E lies on AC such that OED is a straight line.

(a) Find, in terms of a and b, simplifying your answer where possible,

(i)
$$\overrightarrow{CA}$$
 (ii) \overrightarrow{AB} (iii) \overrightarrow{OD}

Given that $CE = \lambda CA$

(b) use a vector method to find the value of λ

(4)

The point P is such that $\overrightarrow{OP} = \mu \overrightarrow{OD}$ where $\mu > 1$ and \overrightarrow{AP} is parallel to \overrightarrow{OB} Given that the area of triangle OCE is 8 cm²

(c) find the area, in cm², of triangle APE

(4)

October 2023/Q9

12.

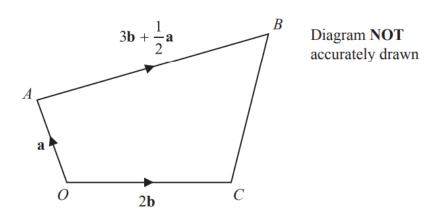


Figure 3

Figure 3 shows quadrilateral OABC

$$\overrightarrow{OA} = \mathbf{a}$$
 $\overrightarrow{AB} = 3\mathbf{b} + \frac{1}{2}\mathbf{a}$ $\overrightarrow{OC} = 2\mathbf{b}$

The point *D* lies on *OB* such that $\overrightarrow{OD} = \frac{3}{5} \overrightarrow{OB}$

(a) Find a simplified expression for \overrightarrow{AD} in terms of **a** and **b**

(3)

The point *E* lies on *CB* such that $\overrightarrow{CE} = k\overrightarrow{CB}$

Given that ADE is a straight line

(b) (i) find the value of k

(4)

(ii) find the ratio AD : DE in the form x : y where x and y are integers.

(2)

October 2024/Q7/P2